

## PRIMARY IDEALS IN $\Gamma$ -SEMIRINGS

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**Abstract:** From an algebraic point of view,  $\Gamma$ - semirings provide the most natural generalization of the theory of semirings. In this paper, we summarize the semiring theoretic results concerning the primary ideals and their radicals to non-commutative  $\Gamma$ - semirings.

**Keywords and Phrases:** Noetherian  $\Gamma$ -semirings, prime ideal, semiprime ideal and primary ideal.

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### 1. Introduction

As a generalization of  $\Gamma$ -rings, the idea of  $\Gamma$ - semiring was presented by Rao [7]. Later it was discovered that  $\Gamma$ - semiring additionally gives an algebraic home to the set of rectangular matrices over a semiring. Dutta and Sardar [2] presented the thought of operator semiring of a  $\Gamma$ - semiring in 2002 and by utilizing the connection between the operator semiring and the  $\Gamma$ - semiring, they enriched the theory of  $\Gamma$ - semiring and demonstrated the outcomes regarding prime ideals and prime radicals of a  $\Gamma$ - semiring via its operator semirings which incorporates various characterizations of prime ideals and prime radicals.

The motivation of this paper is [8] where Sharma et.al received a substitute way to generalize primary ideals from commutative semirings to non-commutative semirings by replacing the role of elements with ideals. In this paper, we define